



RECURSION

Calling a function again before it ends



DIRECT RECURSION

- A function calls itself

```
void f()  
{  
    . . .  
    f();  
    . . .  
}
```



INDIRECT RECURSION

- A chain of function calls that results in a function being called before the first call returns

```
void a()  
{  
    . . .  
    b();  
    . . .  
}
```

```
void b()  
{  
    . . .  
    c();  
    . . .  
}
```

```
void c()  
{  
    . . .  
    d();  
    . . .  
}
```

```
void d()  
{  
    . . .  
    a();  
    . . .  
}
```



REQUIREMENTS FOR RECURSION

- One or more paths through the function where recursion takes place
- One or more paths through the function where recursion *does not* take place. These are the *base cases*
 - may be implicit for simple functions
 - easy to calculate (e.g., a constant value)
- A value, typically an argument, that changes from one function call to the next



RECURSION EXAMPLE: THE FACTORIAL FUNCTION

$0! = 1$ (base case)

$n! = 1 * 2 * 3 * \dots * (n - 1) * n$

$8! = 1 * 2 * 3 * 4 * 5 * 6 * 7 * 8$

$$f(n) = \begin{cases} 1, & n = 0 \text{ (base case)} \\ n(n - 1), & n > 0 \end{cases}$$



THE C++ FACTORIAL FUNCTION

```
int fact(int n)
{
    if (n > 0)
        return n * fact(n - 1); // recursion
    else
        return 1;                // non-recursion
                                   // (base case)
}
```



HOW RECURSION WORKS

